



- ① $\sum i @ V_1$ $i_1 = i_2 + i_4$
- ② $\sum i @ V_2$ $i_2 = i_3 + i_5$
- ③ $\sum i @ V_3$ $i_4 = i_6 + i_{11}$
- ④ $\sum i @ V_4$ $i_5 + i_{11} = i_7 + i_{12}$
- ⑤ $\sum i @ V_5$ $i_3 + i_{12} + i_{10} = 0$
- ⑥ $\sum i @ V_6$ $i_6 = i_8 + i_9$
- ⑦ $\sum i @ V_7$ $i_7 + i_9 = i_{10}$

$$i_1 = \frac{10 - V_1}{R_1}$$

$$i_2 = \frac{V_1 - V_2}{R_2}$$

$$i_3 = \frac{V_2 - V_5}{R_3}$$

$$i_4 = \frac{V_1 - V_3}{R_4}$$

$$i_5 = \frac{V_2 - V_4}{R_5}$$

$$i_6 = \frac{V_3 - V_6}{R_6}$$

$$i_7 = \frac{V_4 - V_7}{R_7}$$

$$i_8 = \frac{V_6}{R_8}$$

$$i_9 = \frac{V_6 - V_7}{R_9}$$

$$i_{10} = \frac{V_7 - V_5}{R_{10}}$$

$$i_{11} = \frac{V_3 - V_4}{R_{11}}$$

$$i_{12} = \frac{V_4 - V_5}{R_{12}}$$

$$\textcircled{1} \quad \frac{10 - V_1}{R_1} = \frac{V_1 - V_2}{R_2} + \frac{V_1 - V_3}{R_4}$$

$$\textcircled{2} \quad \frac{V_1 - V_2}{R_2} = \frac{V_2 - V_5}{R_3} + \frac{V_2 - V_4}{R_5}$$

$$\textcircled{3} \quad \frac{V_1 - V_3}{R_4} = \frac{V_3 - V_6}{R_6} + \frac{V_3 - V_4}{R_{11}}$$

$$\textcircled{4} \quad \frac{V_2 - V_4}{R_5} + \frac{V_3 - V_4}{R_{11}} = \frac{V_4 - V_7}{R_7} + \frac{V_4 - V_5}{R_{12}}$$

$$\textcircled{5} \quad \frac{V_2 - V_5}{R_3} + \frac{V_4 - V_5}{R_{12}} + \frac{V_7 - V_5}{R_{10}} = 0$$

$$\textcircled{6} \quad \frac{V_3 - V_6}{R_6} = \frac{V_6}{R_8} + \frac{V_6 - V_7}{R_9}$$

$$\textcircled{7} \quad \frac{V_4 - V_7}{R_7} + \frac{V_6 - V_7}{R_9} = \frac{V_7 - V_5}{R_{10}}$$

If all of the resistors are the same $1\text{k}\Omega$, then we can simplify:

$$\textcircled{1} \quad 10 - V_1 = V_1 - V_2 + V_1 - V_3$$

$$\checkmark \quad 3V_1 - V_2 - V_3 + 0V_4 + 0V_5 + 0V_6 + 0V_7 = 10$$

$$\textcircled{2} \quad V_1 - V_2 = V_2 - V_5 + V_2 - V_4$$

$$\checkmark \quad V_1 - 3V_2 + 0V_3 + V_4 + V_5 + 0V_6 + 0V_7 = 0$$

$$\textcircled{3} \quad V_1 - V_3 = V_3 - V_6 + V_3 - V_4$$

$$\checkmark \quad V_1 + 0V_2 - 3V_3 + V_4 + 0V_5 + V_6 + 0V_7 = 0$$

$$\textcircled{4} \quad V_2 - V_4 + V_3 - V_4 = V_4 - V_7 + V_4 - V_5$$

$$\checkmark \quad 0V_1 + V_2 + V_3 - 4V_4 + V_5 + 0V_6 + V_7 = 0$$

$$\textcircled{5} \quad V_2 - V_5 + V_4 - V_5 + V_7 - V_5 = 0$$

$$\checkmark \quad 0V_1 + V_2 + 0V_3 + V_4 - 3V_5 + 0V_6 + V_7 = 0$$

$$\textcircled{6} \quad V_3 - V_6 = V_6 + V_6 - V_7$$

$$\checkmark \quad 0V_1 + 0V_2 + V_3 + 0V_4 + 0V_5 - 3V_6 + V_7 = 0$$

$$\textcircled{7} \quad V_4 - V_7 + V_6 - V_7 = V_7 - V_5$$

$$\checkmark \quad 0V_1 + 0V_2 + 0V_3 + V_4 + V_5 + V_6 - 3V_7 = 0$$

$$\begin{bmatrix} 3 & -1 & -1 & 0 & 0 & 0 & 0 \\ 1 & -3 & 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & -3 & 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & -4 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & -3 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & -3 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 & -3 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \\ V_4 \\ V_5 \\ V_6 \\ V_7 \end{bmatrix} = \begin{bmatrix} 10 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

» A USING MATLAB TO SOLVE, WE GET THE FOLLOWING:

A =

3	-1	-1	0	0	0	0
1	-3	0	1	1	0	0
1	0	-3	1	0	1	0
0	1	1	-4	1	0	1
0	1	0	1	-3	0	1
0	0	1	0	0	-3	1
0	0	0	1	1	1	-3

» b

b =

10
0
0
0
0
0
0
0

» x=A\b

x =

6.8750	—	V1
5.6250	—	V2
5.0000	—	V3
5.0000	—	V4
5.0000	—	V5
3.1250	—	V6
4.3750	—	V7

»

CARL, I SHOULD OF HAD A V8 :-)

OR, WE CAN USE PSPICE TO SIMULATE THE CIRCUIT

